

Study of Anisotropy Superconductor using Time-Dependent Ginzburg-Landau Equation

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Abstract

We have observed an anisotropy superconductor which was immersed in vacuum medium in presence of an applied magnetic field. The anisotropy properties of superconductor were related with two principal values of the effective mass of the Cooper pairs, namely m_c along the x -axis and m_{ab} in the yz -plane. Based on the time-dependent Ginzburg-Landau and ψU methods, the problem was solved and made to be the numerical simulation. From study using this numerical simulation, we can find that the anisotropy properties can make the critical field to be lower or higher.

Keywords: anisotropy, superconductor, time-dependent Ginzburg-Landau

1. Introduction

It is well known that the Time Dependent Ginzburg - Landau (TDGL) equations can be used to study the dynamics of superconductivity phenomenon (Tinkham 1996; Du 2005). These equations have nonlinear nature, so it will give results more completely to solve them numerically (Du 2005). One of the numerical solutions has been developed using the gauge invariant variables technique or to be called ψU method (Bolech *et al.* 1995; Gropp *et al.* 1996; Winiecki & Adams 2002). In the last decade, the solution of TDGL equations using ψU method has successfully been used to study the dynamics of superconductivity phenomenon in thin films (Barba *et al.* 2007; Barba *et al.* 2008; Barba-Ortega & Aguiar 2009; Barba-Ortega *et al.* 2010; Barba-Ortega *et al.* 2012; Barba-Ortega *et al.* 2013; Wisodo *et al.* 2013). However, these studies considered the superconductors having isotropy properties.

It is also well known that the high T_c superconductors have anisotropy properties (Tinkham, 1996). These superconductors are viewed as the stack of layers, each layer comprises the ab planes and the c axis is normal to them. The effective mass of the Cooper pairs is different when measured in the ab planes or along the c axis. The results in earlier papers show that the anisotropy properties have influence on superconductivity phenomenon (Hao & Hu 1996; Chapman & Richardson 1998; Achalere & Dey 2008).

In this paper, we study the dynamics of superconductivity phenomenon in an anisotropy superconductor using the TDGL equations and ψU methods. We describe the theoretical formalism and numerical method used for solving the problem in section 2. The results and their analysis are discussed in section 3. Finally, we conclude in section 4.

2. Numerical Methods

2.1 The Time-dependent Ginzburg-Landau Equations

The time-dependent Ginzburg-Landau (TDGL) equations are :

$$\frac{\hbar^2}{2m_s D} \left(\frac{\partial}{\partial t} + i \frac{e_s}{\hbar} \Phi(\mathbf{r}, t) \right) \psi(\mathbf{r}, t) = \frac{\hbar^2}{2m_s} \left(\nabla - i \frac{e_s}{\hbar} \mathbf{A}(\mathbf{r}, t) \right)^2 \psi(\mathbf{r}, t) + |\alpha(T)| \psi(\mathbf{r}, t) - \beta |\psi(\mathbf{r}, t)|^2 \psi(\mathbf{r}, t) \quad (1)$$

$$\begin{aligned} & \frac{1}{\mu_0} \nabla \times (\nabla \times \mathbf{A}(\mathbf{r}, t) - \mu_0 \mathbf{H}_{ext}(\mathbf{r}, t)) \\ &= \frac{\hbar e_s}{2m_s i} \left(\bar{\psi}(\mathbf{r}, t) \nabla \psi(\mathbf{r}, t) - \psi(\mathbf{r}, t) \nabla \bar{\psi}(\mathbf{r}, t) - \frac{2ie_s}{\hbar} |\psi(\mathbf{r}, t)|^2 \mathbf{A}(\mathbf{r}, t) \right) + \sigma \left(-\nabla \Phi(\mathbf{r}, t) - \frac{\partial \mathbf{A}(\mathbf{r}, t)}{\partial t} \right) \end{aligned} \quad (2)$$

where ψ is order parameter, \mathbf{A} and \mathbf{H}_{ext} denote the vector potential and an external magnetic field, e_s and m_s are the effective charge and the effective mass of the Cooper pairs, α dan β are phenomenological parameters, D is a phenomenological diffusion constant, Φ and σ are the electrical potential and conductivity (Bolech *et al.* 1995; Tinkham 1996; Gropp *et al.* 1996; Winiecki & Adams 2002).

In this study, we considered an anisotropic superconductor which is immersed in vacuum medium in presence of an applied magnetic field (The figure 1). Here, an anisotropic superconductor has layered structures, so it has two principal values of m_s , D and σ , namely : m_c , D_c and σ_c along the x -axis and m_{ab} , D_{ab} and σ_{ab} in the yz -plane. The applied magnetic field is assumed in the z -direction, time-dependent, and spatially uniform, so we have $\nabla \times \mathbf{H}_{\text{ext}}(t) = 0$, $\mathbf{B} = B_z(x, y, t)\mathbf{z}$ and $\mathbf{A} = A_x(x, y, t)\mathbf{x} + A_y(x, y, t)\mathbf{y}$.

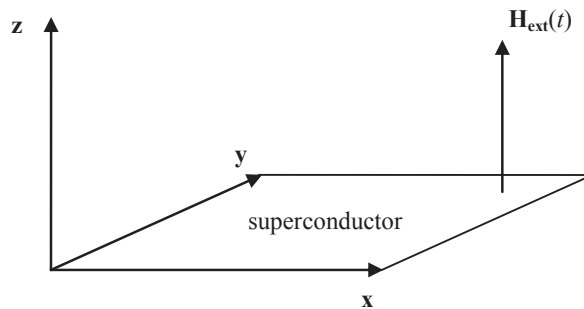


Figure. 1 An anisotropy superconductor in presence of an applied perpendicular uniform magnetic field

If we apply the previous assumption to the time-dependent Ginzburg-Landau, we can obtain :

$$\begin{aligned} & \frac{\hbar^2}{2m_c D_c} \left(\frac{\partial}{\partial t} + i \frac{e_s}{\hbar} \Phi \right) \psi + \frac{\hbar^2}{2m_{ab} D_{ab}} \left(\frac{\partial}{\partial t} + i \frac{e_s}{\hbar} \Phi \right) \psi \\ &= \frac{\hbar^2}{2m_c} \left(\frac{\partial}{\partial x} - i \frac{e_s}{\hbar} A_x \right)^2 \psi + \frac{\hbar^2}{2m_c} \left(\frac{\partial}{\partial y} - i \frac{e_s}{\hbar} A_y \right)^2 \psi + |\alpha| \psi - \beta |\psi|^2 \psi \\ &+ \frac{\hbar^2}{2m_{ab}} \left(\frac{\partial}{\partial x} - i \frac{e_s}{\hbar} A_x \right)^2 \psi + \frac{\hbar^2}{2m_{ab}} \left(\frac{\partial}{\partial y} - i \frac{e_s}{\hbar} A_y \right)^2 \psi + |\alpha| \psi - \beta |\psi|^2 \psi \end{aligned} \quad (3)$$

$$\begin{aligned} & \frac{1}{\mu_0} \frac{\partial}{\partial y} \left(\frac{\partial A_y}{\partial x} - \frac{\partial A_x}{\partial y} \right) \hat{x} - \frac{1}{\mu_0} \frac{\partial}{\partial x} \left(\frac{\partial A_y}{\partial x} - \frac{\partial A_x}{\partial y} \right) \hat{y} \\ &= \frac{\hbar e_s}{2im_c} \left(\bar{\psi} \frac{\partial \psi}{\partial x} - \psi \frac{\partial \bar{\psi}}{\partial x} - \frac{2ie_s}{\hbar} |\psi|^2 A_x \right) \hat{x} - \sigma_c \left(\frac{\partial \Phi}{\partial x} + \frac{\partial A_x}{\partial t} \right) \hat{x} \\ &+ \frac{\hbar e_s}{2im_{ab}} \left(\bar{\psi} \frac{\partial \psi}{\partial y} - \psi \frac{\partial \bar{\psi}}{\partial y} - \frac{2ie_s}{\hbar} |\psi|^2 A_y \right) \hat{y} - \sigma_{ab} \left(\frac{\partial \Phi}{\partial y} + \frac{\partial A_y}{\partial t} \right) \hat{y} \end{aligned} \quad (4)$$

Then, we scale ψ in $\psi_0 = (|\alpha|/\beta)^{1/2}$, t in $\tau_c = \xi_c^2/D_c$, x and y in $\xi_c = (\hbar^2/2m_c|\alpha|)^{1/2}$, A_x and A_y in $A_{0x} = \mu_0 \hbar c_{2c} \xi_c$, Φ in $\Phi_0 = \xi_c A_{0x} / \tau_c$, σ_c and σ_{ab} in $\sigma_{0c} = 1/(\mu_0 \kappa_c^2 D_c)$, and we choose $\Phi = 0$, so we can rewrite equations (3) and (4) in the following form :

$$\left(\frac{1+\varepsilon_m^2\varepsilon_D^2}{\varepsilon_m^2\varepsilon_D^2}\right)\frac{\partial\psi}{\partial t}=\left(\frac{1+\varepsilon_m^2}{\varepsilon_m^2}\right)\left(\frac{\partial}{\partial x}-iA_x\right)^2\psi+\left(\frac{1+\varepsilon_m^2}{\varepsilon_m^2}\right)\left(\frac{\partial}{\partial y}-iA_y\right)^2\psi+2(1-|\psi|^2)\psi \quad (5)$$

$$\begin{aligned} \sigma_c\frac{\partial A_x}{\partial t}\hat{x}+\sigma_{ab}\frac{\partial A_y}{\partial t}\hat{y} &= \frac{1}{2i}\left(\bar{\psi}\frac{\partial\psi}{\partial x}-\psi\frac{\partial\bar{\psi}}{\partial x}-2i|\psi|^2A_x\right)\hat{x}-\kappa_c^2\frac{\partial}{\partial y}\left(\frac{\partial A_y}{\partial x}-\frac{\partial A_x}{\partial y}\right)\hat{x} \\ &+ \frac{1}{2i\varepsilon_m^2}\left(\bar{\psi}\frac{\partial\psi}{\partial y}-\psi\frac{\partial\bar{\psi}}{\partial y}-2i|\psi|^2A_y\right)\hat{y}+\kappa_c^2\frac{\partial}{\partial x}\left(\frac{\partial A_y}{\partial x}-\frac{\partial A_x}{\partial y}\right)\hat{y} \end{aligned} \quad (6)$$

In equations (5) and (6), we define :

$$\xi_c^2=\frac{\hbar^2}{2m_c|\alpha|} \quad \text{and} \quad \xi_{ab}^2=\frac{\hbar^2}{2m_{ab}|\alpha|} \quad (7a)$$

$$\lambda_c^2=\frac{m_c\beta}{\mu_0e_s^2|\alpha|} \quad \text{and} \quad \lambda_{ab}^2=\frac{m_{ab}\beta}{\mu_0e_s^2|\alpha|} \quad (7b)$$

$$\kappa_c^2=\frac{\lambda_c^2}{\xi_c^2} \quad \text{and} \quad \kappa_{ab}^2=\frac{\lambda_{ab}^2}{\xi_{ab}^2} \quad (7c)$$

$$Hc_{2c}=\sqrt{\frac{2}{\mu_0\beta}}|\alpha|\kappa_c \quad \text{and} \quad Hc_{2ab}=\sqrt{\frac{2}{\mu_0\beta}}|\alpha|\kappa_{ab} \quad (7d)$$

$$\varepsilon_m^2=\frac{m_{ab}}{m_c}=\frac{\xi_c^2}{\xi_{ab}^2}=\frac{\lambda_{ab}^2}{\lambda_c^2}=\frac{\kappa_{ab}}{\kappa_c}=\frac{Hc_{2ab}}{Hc_{2c}} \quad (7e)$$

$$\varepsilon_D^2=\frac{D_{ab}}{D_c} \quad (7f)$$

$$\varepsilon_\sigma^2=\frac{\sigma_{ab}}{\sigma_c} \quad (7g)$$

where ξ is the coherence length, λ is the penetration depth, and κ is the Ginzburg-Landau parameter.

The equations (5) and (6) can be solved by the ψU method (Bolech *et al.* 1995; Gropp *et al.* 1996; Winiecki & Adams 2002). In this method, the sample is divided into $N_x \times N_y$ cells, with mesh spacings Δ_x and Δ_y . At the cell, there are three fundamental unknowns, namely ψ , U^x and U^y . The $\psi_{i,j}$ is order parameter at position (x_i, y_j) , with $i = 1, 2, \dots, N_x+1$ and $j = 1, 2, \dots, N_y+1$. The U^x and U^y are the complex link variables and are related to \mathbf{A} by :

$$U_{i,j}^x = \exp\left(-i\int_{x_i}^{x_{i+1}} A_x(\xi, y_j) d\xi\right) \quad \text{with } i=1, 2, \dots, N_x \text{ and } j=1, 2, \dots, N_y+1 \quad (8a)$$

$$U_{i,j}^y = \exp\left(-i\int_{y_j}^{y_{j+1}} A_y(x_i, \eta) d\eta\right) \quad \text{with } i=1, 2, \dots, N_x+1 \text{ and } j=1, 2, \dots, N_y \quad (8b)$$

Using the ψU method and the Euler method and taking $\varepsilon_D = 1$, $\varepsilon_\sigma = 1$, $\sigma_c = \sigma_{ab} = 1$, the equations (5) and (6) can be derived in the following form :

$$\begin{aligned} \psi_{i,j}(t+\Delta t) &= \psi_{i,j}(t) + \Delta t \left(\frac{U_{i,j}^x(t)\psi_{i+1,j}(t) - 2\psi_{i,j}(t) + \bar{U}_{i-1,j}^x(t)\psi_{i-1,j}(t)}{\Delta x^2} \right) \\ &+ \Delta t \left(\frac{U_{i,j}^y(t)\psi_{i,j+1}(t) - 2\psi_{i,j}(t) + \bar{U}_{i,j-1}^y(t)\psi_{i,j-1}(t)}{\Delta y^2} \right) \\ &+ 2\Delta t \left(\frac{\varepsilon_m^2}{1+\varepsilon_m^2} \right) (1-|\psi_{i,j}(t)|^2) \psi_{i,j}(t) \end{aligned} \quad (9)$$

$$U_{i,j}^x(t + \Delta t)\hat{x} = U_{i,j}^x(t)\hat{x} - i\Delta t U_{i,j}^x(t) \text{Im}(U_{i,j}^x(t)\bar{\psi}_{i,j}(t)\psi_{i+1,j}(t))\hat{x} - \kappa_c^2 \frac{\Delta t}{\Delta y^2} U_{i,j}^x(t)(L_{i,j}(t)\bar{L}_{i,j-1}(t) - 1)\hat{x} \quad (10)$$

$$U_{i,j}^y(t + \Delta t)\hat{y} = U_{i,j}^y(t)\hat{y} - \frac{i\Delta t}{\varepsilon_m} U_{i,j}^y(t) \text{Im}(U_{i,j}^y(t)\bar{\psi}_{i,j}(t)\psi_{i,j+1}(t))\hat{y} - \kappa_c^2 \frac{\Delta t}{\Delta x^2} U_{i,j}^y(t)(\bar{L}_{i,j}(t)L_{i-1,j}(t) - 1)\hat{y} \quad (11)$$

where,

$$L_{i,j} = U_{i+1,j}^y \bar{U}_{i,j}^y \bar{U}_{i,j+1}^x U_{i,j}^x \approx \exp(-i\Delta x \Delta y B_{z,i,j}) \quad (12)$$

2.2 The Boundary Conditions

In this study, we considered the superconductor is immersed in vacuum medium in presence of an applied magnetic field, so we have the boundary condition for ψ and \mathbf{A} , namely :

$$\hat{\mathbf{n}} \cdot \left[-i\nabla - \frac{e_s}{\hbar} \mathbf{A} \right] \psi = 0 \quad (13)$$

$$B_{ext,z} = B_z = \frac{\partial A_y}{\partial x} - \frac{\partial A_x}{\partial y} \quad (14)$$

where $\hat{\mathbf{n}}$ denotes the unit normal to the superconductor–vacuum interface.

If we apply the previous research assumptions and scale ψ in $\psi_0 = (|\alpha|/\beta)^{1/2}$, x and y in $\xi_c = (\hbar^2/2m_c|\alpha|)^{1/2}$, A_x and A_y in $A_{0x} = \mu_0 H c_{2c} \xi_c$, B_z and $B_{ext,z}$ in $\mu_0 H c_{2c}$, H_z and $H_{ext,z}$ in $H c_{2c}$, then we can use the ψU method and the Euler method to rewrite equations (13) and (14) in the following form :

$$\begin{aligned} \text{at } i = 1 : \quad & \psi_{1,j}(t) = U_{1,j}^x(t) \psi_{2,j}(t) \\ & \psi_{N_x+1,j}(t) = \bar{U}_{N_x,j}^x(t) \psi_{N_x,j}(t) \end{aligned} \quad (15a)$$

$$\text{at } i = N_x + 1 : \quad \psi_{i,1}(t) = U_{i,1}^y(t) \psi_{i,2}(t) \quad (15b)$$

$$\text{at } j = 1 : \quad \psi_{i,N_y+1}(t) = \bar{U}_{i,N_y}^y(t) \psi_{i,N_y}(t) \quad (15c)$$

$$\text{at } j = N_y + 1 : \quad (15d)$$

and

$$\begin{aligned} \text{at } i = 1 : \quad & U_{1,j}^y \approx U_{2,j}^y \bar{U}_{1,j+1}^x U_{1,j}^x \exp(-i\Delta x \Delta y H_{ext,z}) \\ & U_{N_x+1,j}^y \approx U_{N_x,j}^y U_{N_x,j+1}^x \bar{U}_{N_x,j}^x \exp(-i\Delta x \Delta y H_{ext,z}) \end{aligned} \quad (16a)$$

$$\text{at } i = N_x + 1 : \quad U_{i,1}^x \approx \bar{U}_{i+1,1}^y U_{i,1}^y U_{i,2}^x \exp(-i\Delta x \Delta y H_{ext,z}) \quad (16b)$$

$$\text{at } j = 1 : \quad U_{i,N_y+1}^x \approx U_{i+1,N_y}^y \bar{U}_{i,N_y}^y U_{i,N_y}^x \exp(-i\Delta x \Delta y H_{ext,z}) \quad (16c)$$

$$\text{at } j = N_y + 1 : \quad (16d)$$

2.3 The Numerical Simulation

We begin the numerical simulation with determining the value of N_x , N_y , Δx , Δy , Δt , κ_c and ε_m . We also assume the initial condition of superconductor as in a perfect Meissner state, so we have $H_{ext,z} = 0$, $\psi_{i,j} = 1$, $U_{i,j}^x = 1$ and $U_{i,j}^y = 1$. Then, $H_{ext,z}$ is increased linearly with time and with small intervals of $\Delta H_{ext,z}$. When we have a new value of $H_{ext,z}$, we compute the new values of $\psi_{i,j}$, $U_{i,j}^x$ and $U_{i,j}^y$ using equations (9), (10), (11), (15) and (16).

Using this numerical simulation, we can also make magnetization curves. Magnetization can be calculated from :

$$(17)$$

where M_z is scaled in $H c_{2c}$ and B_z is calculated by equation (12):

3. Results and Discussion

We try to run the numerical simulation with choosing five cases, namely : $\varepsilon_m = 1.0$, $\varepsilon_m = 0.5$, $\varepsilon_m = 0.8$, $\varepsilon_m = 1.3$, and $\varepsilon_m = 2.0$. For each case, the values of another input are the same, namely : $N_x = 32$, $N_y = 32$, $\Delta_x = 0.5$, $\Delta_y = 0.5$, $\Delta t = 0.010$, $\Delta H_{ext,z} = 0.000001$, and $\kappa_c = 2.0$. When $\varepsilon_m = 1.0$, it is the isotropy superconductor case and the others are the anisotropy superconductor cases.

In figure 2(a), we show the square modulus order parameter curve as a function of magnetic field $|\overline{\psi}|^2 - H_{ext}$ in the five cases. We can see in the figure, the $|\psi(x,y)|^2$ will completely vanish at the higher value of the applied field $H_{ext,z}$ when the value of ε_m increases. It means, by increasing ε_m the value of the surface nucleation field H_{c3} will be higher.

In figure 2(b), we show the magnetization curve as a function of magnetic field $M-H_{ext}$ in the five cases. We can see, as increasing the applied field $H_{ext,z}$, the magnetization curve will decrease until the minimum value, then increase until the zero value. When the value of ε_m increases, we find that the minimum value will be located at the higher value of the applied field $H_{ext,z}$ if $\varepsilon_m \leq 1$ and at the lower value of the applied field $H_{ext,z}$ if $\varepsilon_m \geq 1$. We also find that the zero value will be located at the higher value of the applied field $H_{ext,z}$ when the value of ε_m increases. It means, by increasing ε_m , if $\varepsilon_m \leq 1$ the value of the lower critical field H_{c1} will be higher and if $\varepsilon_m \geq 1$ the value of H_{c1} will be lower. It also means, by increasing ε_m , the value of H_{c3} will be higher.

We show the distribution of the square modulus order parameter $|\psi(x,y)|^2$ on sample for five cases and for the several values of the applied field $H_{ext,z}$ in the figure 3-7. From these figures, we can see that in the low applied field $H_{ext,z}$, $|\psi(x,y)|^2$ has a high value. As increasing $H_{ext,z}$, the magnetic field will penetrate into sample to form vortex and $|\psi(x,y)|^2$ will decrease. When the value of ε_m increases, we find that $|\psi(x,y)|^2$ will vanish in the higher value of the applied field $H_{ext,z}$, the vortex is formed in the higher value of the applied field $H_{ext,z}$ if $\varepsilon_m \leq 1$ and in the lower value of the applied field $H_{ext,z}$ if $\varepsilon_m \geq 1$. Once again, these results mean that by increasing ε_m , the value of H_{c3} will be higher, if $\varepsilon_m \leq 1$ the value of H_{c1} will be higher and if $\varepsilon_m \geq 1$ the value of H_{c1} will be lower.

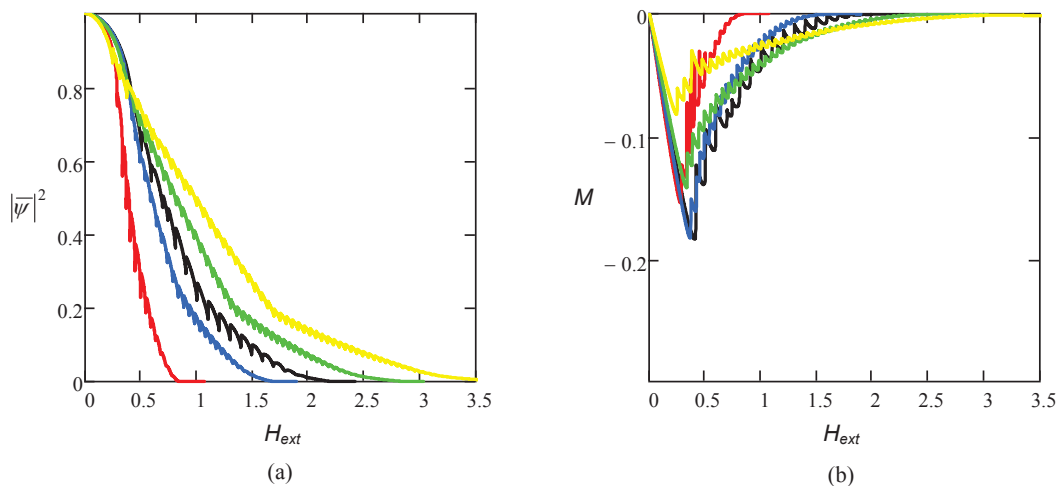


Figure 2. Plot of (a) $|\overline{\psi}|^2 - H_{ext}$ and (b) $M-H_{ext}$ in the cases of :

— : $\varepsilon_m = 0.5$ — : $\varepsilon_m = 0.8$ — : $\varepsilon_m = 1.0$ — : $\varepsilon_m = 1.3$ — : $\varepsilon_m = 2.0$

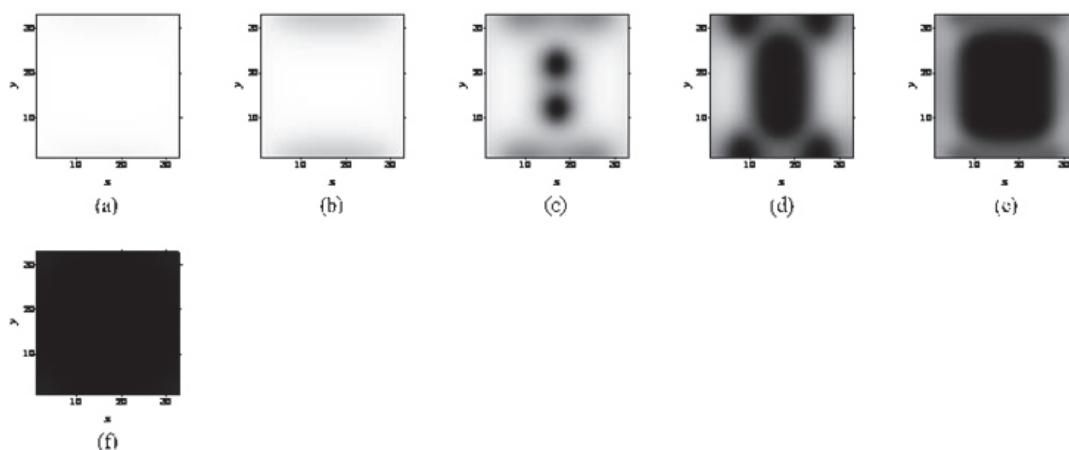


Figure 3. Plot of $|\psi(x,y)|^2$ in the case of $\varepsilon_m=0.5$ and (a) $H_{ext,z}=0.10$ (b) $H_{ext,z}=0.20$ (c) $H_{ext,z}=0.30$ (d) $H_{ext,z}=0.40$ (e) $H_{ext,z}=0.50$ (f) $H_{ext,z}=0.80$
The white and the black colours indicate $|\psi(x,y)|^2=1$ and $|\psi(x,y)|^2=0$.

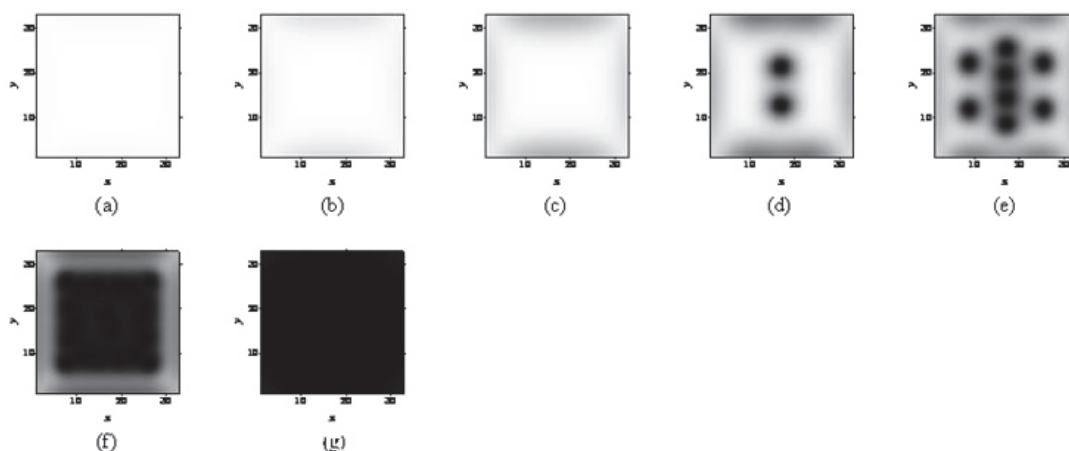


Figure 4. Plot of $|\psi(x,y)|^2$ in the case $\varepsilon_m=0.8$ and (a) $H_{ext,z}=0.10$ (b) $H_{ext,z}=0.20$ (c) $H_{ext,z}=0.30$ (d) $H_{ext,z}=0.40$ (e) $H_{ext,z}=0.50$ (f) $H_{ext,z}=0.80$ (g) $H_{ext,z}=1.60$
The white and the black colours indicate $|\psi(x,y)|^2=1$ and $|\psi(x,y)|^2=0$.

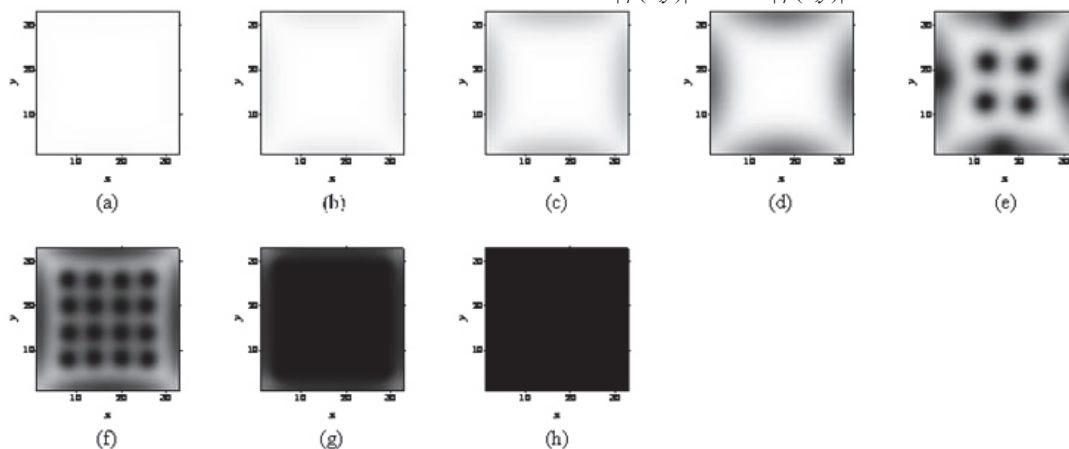


Figure 5. Plot of $|\psi(x,y)|^2$ in the case of $\varepsilon_m=1.0$ and (a) $H_{ext,z}=0.10$ (b) $H_{ext,z}=0.20$ (c) $H_{ext,z}=0.30$ (d) $H_{ext,z}=0.40$ (e) $H_{ext,z}=0.50$ (f) $H_{ext,z}=0.80$ (g) $H_{ext,z}=1.60$ (h) $H_{ext,z}=2.20$.
The white and the black colours indicate $|\psi(x,y)|^2=1$ and $|\psi(x,y)|^2=0$.

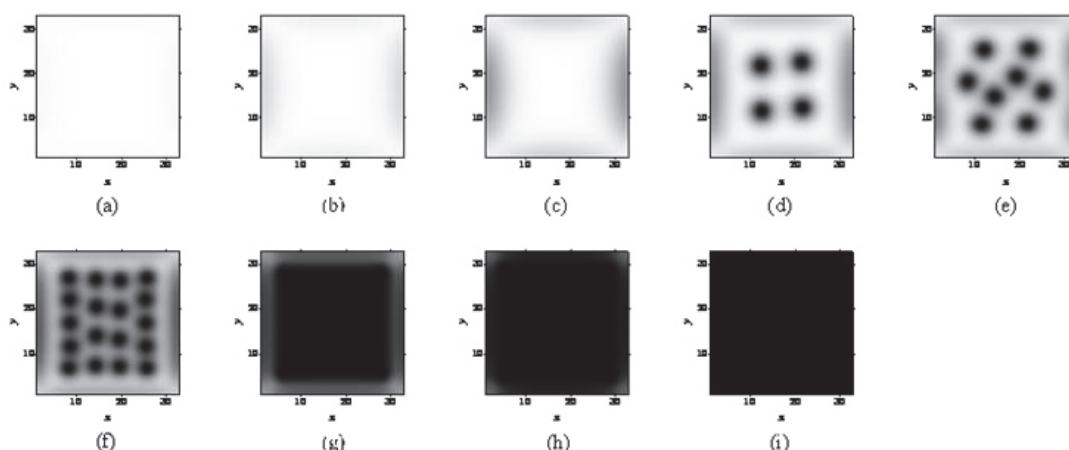


Figure 6. Plot of $|\psi(x,y)|^2$ in the case of $\varepsilon_m=1.3$ and (a) $H_{ext,z}=0.10$ (b) $H_{ext,z}=0.20$ (c) $H_{ext,z}=0.30$ (d) $H_{ext,z}=0.40$ (e) $H_{ext,z}=0.50$ (f) $H_{ext,z}=0.80$ (g) $H_{ext,z}=1.60$ (h) $H_{ext,z}=2.20$ (i) $H_{ext,z}=2.80$.
The white and the black colours indicate $|\psi(x,y)|^2=1$ and $|\psi(x,y)|^2=0$.

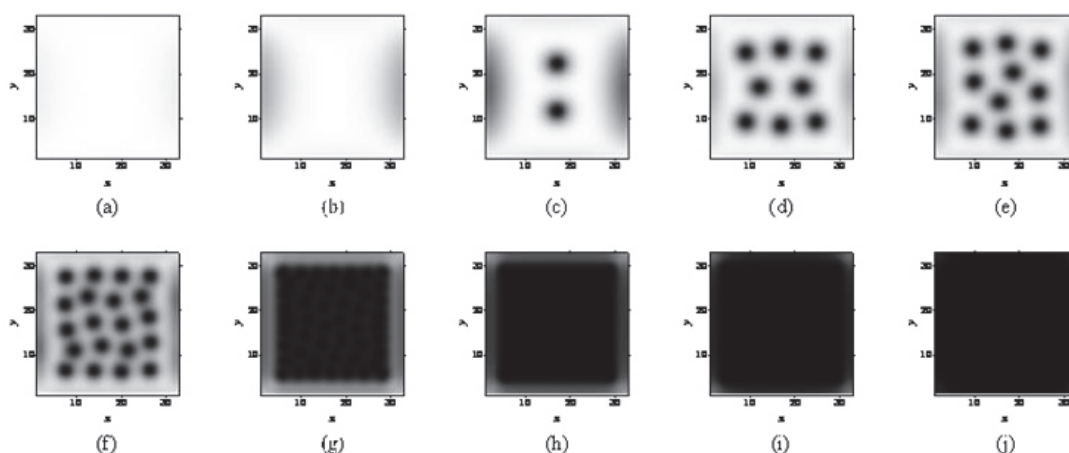


Figure 7. Plot of $|\psi(x,y)|^2$ in the case of $\varepsilon_m=2.0$ and (a) $H_{ext,z}=0.10$ (b) $H_{ext,z}=0.20$ (c) $H_{ext,z}=0.30$ (d) $H_{ext,z}=0.40$ (e) $H_{ext,z}=0.50$ (f) $H_{ext,z}=0.80$ (g) $H_{ext,z}=1.60$ (h) $H_{ext,z}=2.20$ (i) $H_{ext,z}=2.80$ (j) $H_{ext,z}=3.50$.
The white and the black colours indicate $|\psi(x,y)|^2=1$ and $|\psi(x,y)|^2=0$.

4. Conclusion

We have made a numerical solution of the Time Dependent Ginzburg - Landau (TDGL) equations for anisotropic superconductor using ψU methods. From this simulation, if we set κ_c in the fixed value and increase ε_m , we will obtain the value of H_{c3} will be higher and the value of H_{c1} will be higher if $\varepsilon_m \leq 1$ and will be lower if $\varepsilon_m \geq 1$.

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